

OVERVIEW

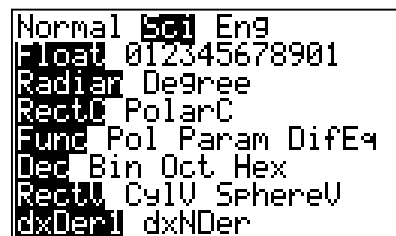
The intent of this material is to provide instruction for the TI-86 graphing calculator that may be used in conjunction with the second edition of Gary Rockswold's *College Algebra Through Modeling and Visualization*. It includes specific keystrokes needed to work several examples from the text. Students are also advised to consult the *Graphing Calculator Guidebook* provided by the manufacturer. These instructions are not meant to replace the manual that accompanies your calculator but rather they are an attempt to simplify some of the instructions you might find there.

DISPLAYING NUMBERS IN SCIENTIFIC NOTATION

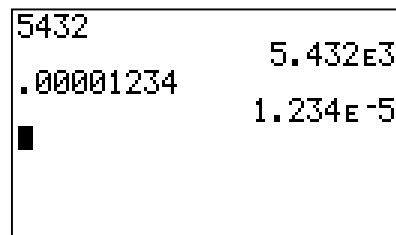
To change numbers entered on the home screen to scientific notation, you must change the setting of the calculator to scientific mode (Sci).

To display numbers in scientific notation:

1. Locate "MODE" above the **MORE** key in the first row on your calculator. Press **2nd** **MODE**.
2. Use the right arrow cursor key to highlight "Sci".
3. Press **ENTER** to select this mode.
4. Press **2nd** **QUIT** to return to the home screen.



Type in the numbers 5432 and 0.00001234, pressing **ENTER** after each number. You should see the screen similar to the one on the right.

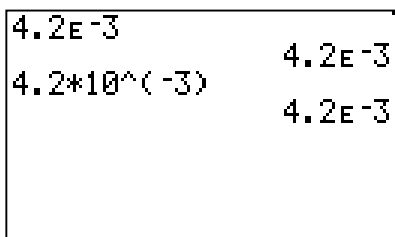


ENTERING NUMBERS IN SCIENTIFIC NOTATION

Numbers can be entered into the calculator in scientific notation.

To enter a number in scientific notation:

1. Locate the **EE** key in the fifth row of your calculator.
2. Enter the number that precedes the powers of ten.
3. Press **EE** followed by the exponent (or power of ten).
4. Press **ENTER**



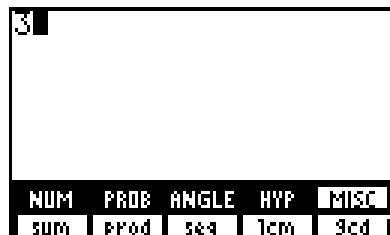
To enter 4.2×10^{-3} , use the following key strokes: **4.2** **EE** **- 3** OR **4.2** **×** **10** **^** **- 3**. Follow either choice by pressing the **ENTER** key. Both examples are shown in the diagram on the left.

ENTERING MATHEMATICAL EXPRESSIONS

Several expressions are evaluated in Example 7, Section 1.1. The keystrokes below allow you to use the graphing calculator to evaluate these expressions.

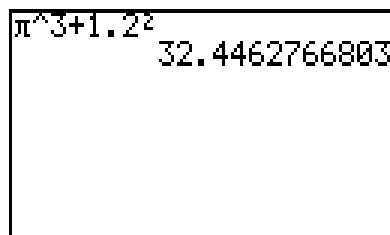
1) To evaluate $\sqrt[3]{131}$, use the following keystrokes:

- Type the root of the expression, in this case 3
- Locate “Math” over the multiplication key. Press 2ND MATH to access the MATH menu.
- Press **F5** to access the MISC (miscellaneous) menu.
- You should see **gcd** in the bottom row of your screen. This indicates that there are more items in the MISC menu. Press MORE to access those additional features. Notice that the menu options on the bottom of the calculator screen have changed.
- Press **F4** to select the \sqrt{x} option. Now type 131.
- Press **ENTER**.



2) To evaluate $\pi^3 + 1.2^2$, use the following keystrokes:

- Locate π over the ^ symbol in the fourth row of your calculator. The ^ symbol is used to raise a number or variable to a power.
- Locate the x^2 key at the start of the sixth row of your calculator.
- Type **2ND** π **^** 3 + 1.2 **x²**
- Press **ENTER**.



3) To calculate $|\sqrt{3} - 6|$, use the following keystrokes to access the absolute value function:

- Use the keystrokes **2ND** **MATH** to access the MATH menu.
- Press **F1** to access the MATH NUM menu.
- Press **F5** to select *abs*.
- Locate the \sqrt{x} over the x^2 key.
- Type (**2ND** \sqrt{x} 3 - 6). Press **ENTER**.



CALCULATING ONE VARIABLE STATISTICS

In Example 2, Section 1.2, the mean, median, minimum and maximum values for a data set are found using the built in statistical capabilities of the graphing calculator.

To calculate one variable statistics:

1. To enter the data from Example 2 into your calculator begin by locating the STAT menu found above the plus sign in the next to last row of your calculator.

2. Press **2ND** **STAT** to access the statistics menus.

3. Press **F2** (EDIT) to enter the data. Enter each value followed by the **ENTER** key. Your list will look like the screen on the right.

xStat	yStat	fStat	1
5.70	-----	-----	
4.20			
3.70			
2.40			
1.70			
1.40			
xStat(1)=5.7			
<	>	NAMES	" OPS

4. Press **2ND** **QUIT** then **2ND** **STAT** .

5. Press **F1** to access the Calculations Menu

6. Press **F1** again to select OneVa. This function will analyze the data in the xStat list.

7. Locate the LIST menu over the subtraction key in the third row up from the bottom.

8. Press **2nd** **LIST**, **F3** to open the lists window

9. Press **F2** to select xStat then **ENTER**.

1-Var Stats			
$\bar{x}=3.18$			
$\Sigma x=38.20$			
$\Sigma x^2=161.76$			
$\downarrow Sx=1.91$			
↓			
<	>	NAMES	EDIT OPS
fStat	xStat	yStat	

10. Note the ↓ in the lower left hand corner of your calculator screen. This indicates that there are other values to be viewed. Use the down cursor arrow to view these values.

As you scroll through the data you will find that the mean of the data is 3.18, the median (noted as Med) is 2.95, minX is .8 and maxX is 5.9.

SUMMARY: CALCULATING ONE-VARIABLE STATISTICS

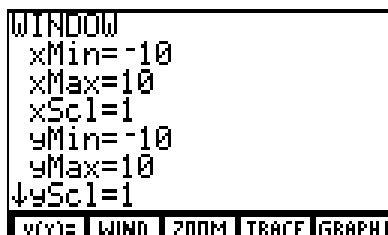
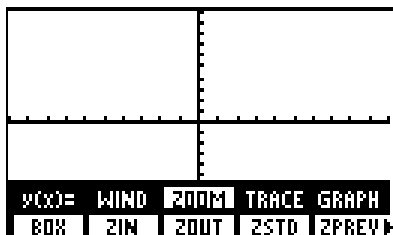
1. Press **2ND** **STAT** **F2** to enter the data in xStat.
2. Press **2ND** **QUIT** then **2ND** **STAT** .
3. Press **F1** then **F1** again to select OneVa.
4. Press **2nd** **LIST**, **F3** **F2** to select xStat then **ENTER**.
5. Note the ↓ in the lower left hand corner of your calculator screen indicating there are other values to be viewed. Use the down cursor arrow to view these values.

SETTING THE VIEWING RECTANGLE

Example 7, Section 1.2, asks you to show a standard viewing rectangle and then to change the window settings in the graphing window screen. The standard viewing window (or default setting of your calculator) shows the x and y axis as $[-10,10,1]$ by $[-10,10,1]$.

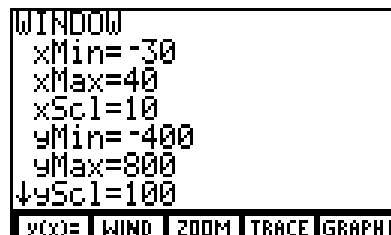
To set the window to the standard setting:

1. Locate the GRAPH key in the third row from the top on your calculator keypad.
2. Press **GRAPH** then **F3** to access the ZOOM menu.
3. Press **F4** to select ZSTD (or the standard window settings) as seen below.
4. Press **2ND** **M5** to see the graphing window you have set.



To change a viewing rectangle:

1. Press **GRAPH** then **F2** to access the WIND setup.
2. Enter the values for the window in which to view your graph. In this example we use $[-30,40,10]$ by $[-400, 800, 100]$.
3. Press **F5** to see the graphing window you have set.



MAKING A SCATTERPLOT

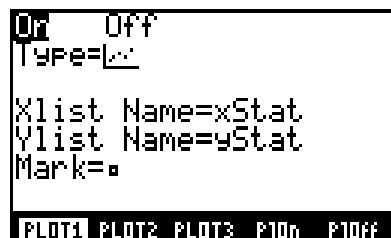
Example 8, Section 1.2 asks us to make a scatterplot using the points $(-5, 5)$, $(-2, 3)$, $(1, -7)$ and $(4, 8)$.

To make a scatter plot:

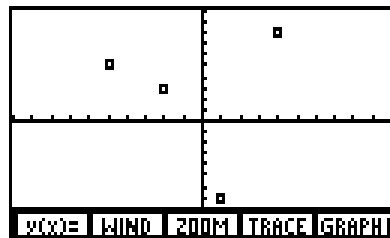
1. Press **2ND** **STAT** then **F2** (EDIT) to enter the points.
2. Enter the x values for xStat using the same method described in an earlier section on “calculating one variable statistics”. When you are finished entering the x values use the right cursor arrow to move to the yStat column and enter the y values.
3. Press **2ND** **STAT** **F3** to access the PLOT options.
4. Press **F1** to select **PLOT1**. Select ON by pressing **ENTER**. This will enable you to plot points in your graphing window.

xStat	yStat	fStat	2
-5.00	5.00	-----	
-2.00	3.00		
1.00	-7.00		
4.00	8.00		

yStat(5) =			
{	}	NAMES	" OPS



- Set an appropriate viewing window.
- Press the **GRAPH** key located in the third row, then **F5** to view your scatterplot as seen below.



SUMMARY: MAKING A SCATTERPLOT

- Press **2ND** **STAT** **F2**
- Enter your data in the xStat and yStat column. .
- Press **2ND** **STAT** **F3** to access the PLOT options.
- Press **F1** to select **PLOT1**. Select ON by pressing **ENTER**.
- Press the **GRAPH** key then **F5** to view your scatterplot. Adjust your viewing window if necessary.

ENTERING A FORMULA FOR A FUNCTION

To enter the formula for a given function f :

- Press **GRAPH**.
- Press **F1** to select the $y(x)=$ screen.
- Enter the formula you wish to use. To enter the variable x in your formula use the **x-VAR** key located in the second row of your calculator.

To enter the function $f(x) = 2x^2 - 3x + 7$ once you are in the $y(x) =$ screen use the following keystrokes:

2 **x-VAR** **^** **2** **-** **3** **x-VAR** **+** **7**



GRAPHING A FUNCTION

Since a picture is worth a thousand words it is often to our advantage to graph functions to learn more about them. Suppose we wished to graph the function $f(x) = x^2 - 4$.

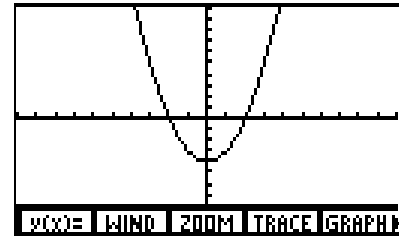
To graph a function:

- Press **GRAPH**, then **F1** to select the $y(x)=$ screen.. If there is already a function in the $y1=$ spot and you wish to remove this function, press the **CLEAR** key.



2. Enter the function you wish to graph.
3. Press $\boxed{2^{ND}}$ $\boxed{M5}$ to display the graph of your function.

The equal sign after y1 should appear highlighted. This indicates that the function is “on” and that it will be graphed. If the equal sign is not “on”, place the cursor over it and press \boxed{ENTER} .



SUMMARY: GRAPHING A FUNCTION

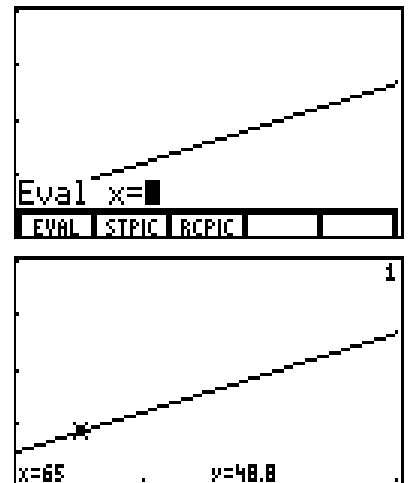
1. To graph a function press \boxed{GRAPH} , then $\boxed{F1}$.
2. Enter the function you wish to graph.
3. Press $\boxed{2^{ND}}$ $\boxed{M5}$ to display the graph of your function.

EVALUATING A FUNCTION GRAPHICALLY

In Example 7, Section 1.3, we evaluate the function $f(x) = 0.72x + 2$ at $x = 65$ graphically using the trace feature of the graph.

To evaluate a function:

1. Enter the formula into the $y1 =$ screen.
2. Graph the function in an appropriate viewing window. In this example we used $[60,90,10]$ by $[40, 80, 10]$.
3. Notice that the last choice on the bottom row is $\boxed{GRAPH \blacktriangleright}$. The \blacktriangleright indicates that there are more choices to view. To access those choices press the \boxed{MORE} key. Notice that the options on the bottom of the screen change.
4. Press the \boxed{MORE} key until you see \boxed{EVAL} in the lower left corner.
5. Press $\boxed{F1}$ to select the evaluation feature.
6. Enter the value for x (in this case $x = 65$) then press \boxed{ENTER} to view the screen on the right.



SUMMARY: EVALUATING A FUNCTION GRAPHICALLY

1. Graph the function in an appropriate viewing window.
2. Press the \boxed{MORE} key until you see \boxed{EVAL} in the lower left corner.
3. Press $\boxed{F1}$ to select the evaluation feature.
4. Enter the value for x where the function should be evaluated.
5. Press \boxed{ENTER} .

MAKING A TABLE

In Example 7, Section 1.3, a table of values is requested.

To create a table:

1. Enter the equation $Y_1 = .72X + 2$ using the instructions presented earlier for entering a formula for a function
2. Press the **TABLE** button located in the third row from the top on your calculator. You should see the screen located on your right. In this screen we have two options: **TABLE** which will bring us right to the table screen and **TBLST** which is a table setup editor. Press the **F1** key to access the table. Press the **F2** key to access the table setup editor.
3. Press the **F2** key. This window allows us to set the parameters for our table.
4. With the cursor blinking after TblStart = , type 60 and press **ENTER**
5. On the $\Delta Tbl = 1$ you can change the increments of the independent variable displayed in the table. We will leave this at 1 for this problem. The values of Y_1 at $x = 60, 61, 62, \dots$ will be shown in the table. Press **ENTER**.
6. Make sure that **AUTO** is highlighted next to Indpnt:. This indicates that the calculator will automatically generate the x values based on the information entered in steps 3 and 4 above. If **ASK** is highlighted, use the left arrow cursor key to position the cursor over **AUTO** and press **ENTER**. (ASK displays an empty table and allows you to enter x values. As each value is added to the independent variable column the corresponding value for the dependent variable is calculated and displayed).

Plot1	Plot2	Plot3
Y1=.72x+2		
TABLE	TBLST	

TABLE SETUP	
TblStart=	60
$\Delta Tbl=$	1
Indpnt:	AUTO Ask
TABLE	

x	Y1
60	45.2
61	45.92
62	46.64
63	47.36
64	48.08
65	48.8

Y1=.72x+2

TBLST	SELC	x	y
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7. Press **F1** to display the table. You can scroll through the x and y values by using the arrow keys.

SUMMARY: MAKING A TABLE OF A FUNCTION

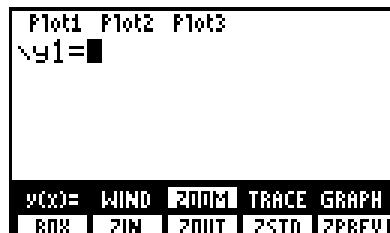
1. Enter the formula for the function.
2. Press the **TABLE**
3. Press the **F2** key to choose **TBLST** to set the parameters for the table.
4. Press **F1** to display the table.

SQUARING A VIEWING RECTANGLE

The window in which you view your graphs on the calculator is a rectangle. In the $[-10,10,1]$ by $[-10,10,1]$ standard viewing window you will notice that tick marks on the x axis are further apart than the tick marks on the y axis. This leads to the distortion of some graphs. A circle does not appear truly circular in the standard viewing window and the line $y = x$ does not make a 45° angle with the horizontal axis.

To square the viewing window:

1. Press the **GRAPH** key.
2. Press **F3** to access the **ZOOM** menu. This will display the screen shown on the right. Notice that the last choice on the bottom row is **ZPREV** \blacktriangleright . The \blacktriangleright indicates that there are more choices that we can view in the ZOOM menu.
3. To access these choices press the **MORE** key. The menu options on the bottom of the calculator screen have changed.
4. Press **F2** to choose **ZSQR** to square the viewing rectangle.



SUMMARY: SQUARING A VIEWING RECTANGLE

1. Press the **GRAPH** key.
2. Press **F3** to access the **ZOOM** menu.
3. Press the **MORE** key.
4. Press **F2** to choose **ZSQR** to square the viewing rectangle.

PLOTTING DATA AND AN EQUATION

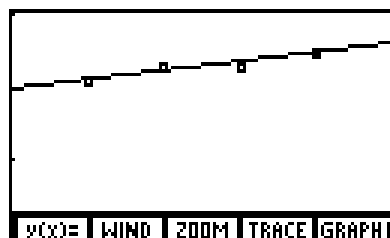
In Example 1, Section 2.1, we plot data and graph a modeling function in the same viewing window. Refer back to earlier instructions for creating a scatterplot and line graph as needed.

1. Begin by entering the x values in xStat and the y values in yStat as seen in the first screen shot below. (Refer to earlier instructions “Making a Scatterplot” if needed.)
2. Turn STAT PLOTS on.
3. Enter the formula $Y_1 = .062x - 122.57$
4. Set an appropriate viewing window. In this case use $[1993,1998,1]$ by $[0,1.5,.5]$ as seen in the middle screen below.
5. Now press **F5** to access GRAPH to have both the scatterplot and the graph of Y_1 displayed in the same viewing window as seen in the screen shot on the far right.

xStat	yStat	fStat	2
1994	1.05	-----	
1995	1.13		
1996	1.14		
1997	1.24		

yStat(5) =			
{	}	NAMES	"
		DPS	1

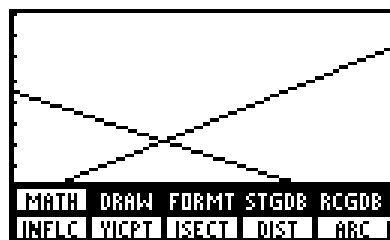
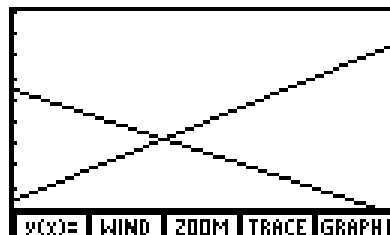
WINDOW
xMin=1993
xMax=1998
xScl=1
yMin=0
yMax=1.5
↓yScl=.5
WIND ZOOM TRACE GRAPH



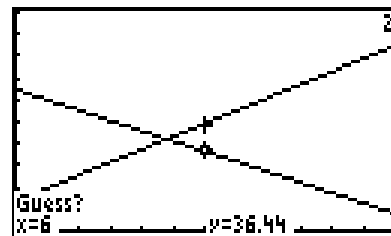
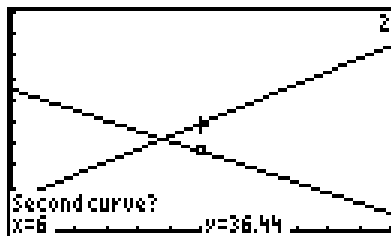
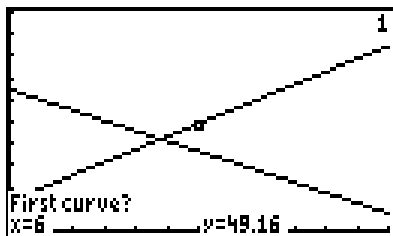
LOCATING THE POINT OF INTERSECTION

In Example 1, Section 2.3 we find the point of intersection of two lines. Given the two functions $f(x) = 5.91x + 13.7$ and $g(x) = -4.71x + 64.7$ we will locate the point of intersection of these two functions.

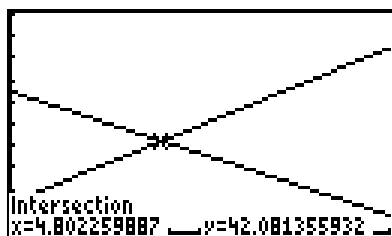
1. Enter the function given by $f(x)$ as Y_1 . Press ENTER.
2. Enter the function given by $g(x)$ as Y_2 .
3. Set the viewing window to $[0,12,1]$ by $[0,100,10]$
4. Press **F5** to see a graph of Y_1 and Y_2 as seen on the right.
5. Notice that the last choice on the bottom row is **GRAPH ▸**. Recall that the ▸ indicates that there are more choices to view.
6. Press **MORE**
7. Press **F1** to access the **MATH** menu
8. Press **MORE**. You should now see a screen similar to the one shown on the right.
9. Press **F3** to select ISECT. This will allow us to find the intersection between two functions.



10. A graph is displayed with a blinking cursor and “First curve ?” at the bottom of the screen. This is seen in the sequence of graphs below.
11. Move your cursor closer to the point of intersection of the two functions and press **ENTER**.
12. The cursor moves to the second function and “Second curve ?” is displayed. Press **ENTER**.



13. You will now see a screen with “Guess ?” . Press **ENTER**.
14. You can now see that the two lines intersect at the point $(4.802259887, 42.081355932)$ as shown in the figure below.



SUMMARY: FINDING A POINT OF INTERSECTION

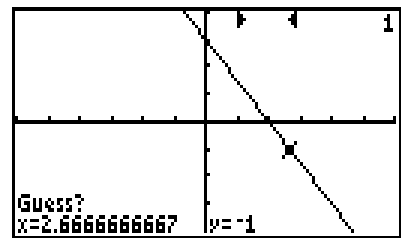
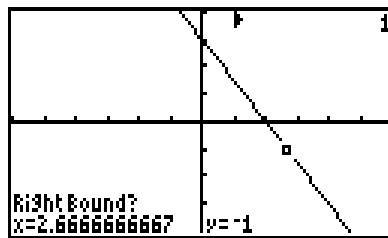
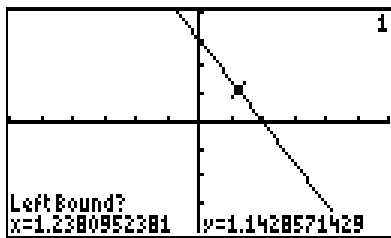
1. Enter and graph the two functions in an appropriate viewing window
2. Notice that the last choice on the bottom row is **GRAPH ▸**. Press **MORE**
3. Press **F1** to access the **MATH** menu. Press **MORE**.
4. Press **F3** to select ISECT.
5. In the “First curve ?” screen move your cursor closer to the point of intersection of the two functions and press **ENTER**
6. In the “Second curve ?” screen press **ENTER**.
7. In the “Guess ?” screen press **ENTER**.
8. The cursor is now located at the intersection with the cursor coordinates displayed at the bottom of the screen.

LOCATING A ROOT OF A FUNCTION

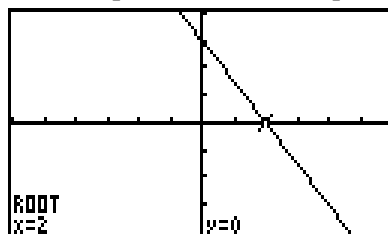
In Example 3, Section 2.4, we locate an x -intercept or *root* of a function $f(x) = 1 - x - \left(\frac{1}{2}x - 2\right)$.

To find the x – intercept or *root* of a function

1. Enter the formula for $f(x)$ as Y_1 .
2. Set the viewing widow for your graph to $[-6,6,1]$ by $[-4,4,1]$ and graph Y_1 .
3. The last choice on the bottom row is **GRAPH ▸**. Press **MORE** then press **F1** to access the **MATH** menu.
4. Press **F1** again to select ROOT.
5. A graph is displayed with a blinking cursor and “Left Bound?” at the bottom of the screen. This is seen in the sequence of graphs below. Move your cursor closer to the x – axis, making sure that it is to the left of the x - intercept. Press **ENTER**.
6. You are now asked for a “Right Bound?”. Move the cursor to the right of the of the x -intercept and press **ENTER**.
7. You will now see a screen with “Guess ?”. Press **ENTER**.



8. The calculator determines that the x -intercept or *root* of this equation is $(2,0)$ as seen in the screen below.



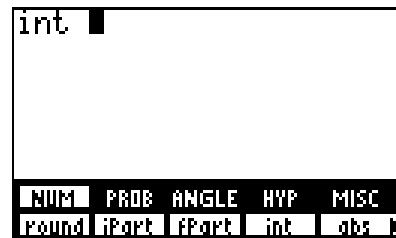
SUMMARY: LOCATING THE ROOT OF A FUNCTION

1. Graph the function in an appropriate viewing window
2. Press the **MORE** key
3. Press **F1** to access the **MATH** menu.
4. Press **F1** to select **ROOT**.
5. In the “Left Bound?” screen place your cursor to the left of the x – intercept and press **ENTER**.
6. In the “Right Bound?” screen place your cursor to the right of the x – intercept and press **ENTER**.
7. In the “Guess ?” screen press **ENTER**.
8. The calculator now displays the root of the equation at the bottom of the screen.

ACCESSING THE GREATEST INTEGER FUNCTION

To access the greatest integer:

1. Use the keystrokes **2ND** **MATH** to access the MATH menu .
2. Press **F1** to access the MATH NUM menu.
3. Press **F4** to select *int*. This function will return the greatest integer less than or equal to the value you enter.



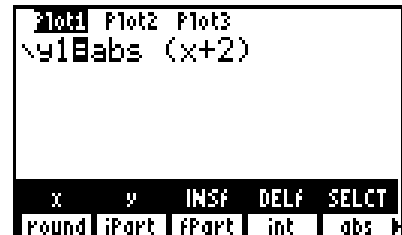
ACCESSING THE ABSOLUTE VALUE

In Example 4, Section 2.5 the absolute value was used to graph $f(x) = |x + 2|$. To graph this function we need to be able to access the absolute value on the calculator.

To access the absolute value:

1. Follow the first 2 steps from the preceding instructions to access the MATH NUM menu.
2. Press **F5** to select *abs*. This function returns the absolute value or the magnitude of the value you enter.

To graph $f(x)$ use the following keystrokes at the cursor prompt for $Y_1 =$ **2ND** **MATH** **F1** **F5** to display the abs. Use parenthesis around $x + 2$.



FINDING THE LINE OF LEAST-SQUARES FIT

In Example 3, Section 2.6, the line of least squares fit for the points (1,1), (2,3) and (2,4) is found.

To find the line of least-squares fit:

1. Enter the points in xStat and yStat as if to create a scatterplot.
2. Press **2ND** **QUIT** to leave the lists you have created.
3. Press **2ND** **STAT** followed by **F1** to access the CALC (calculations) menu.
4. Press **F3** to access the LinR (linear regression function) This function fits the equation $y = a + bx$ to the data. The format required by this function is LinR(xstat, ystat, y1).
5. Use the following keystrokes **(** **2ND** **LIST** **NAMES** **F2** **F3** **2ND** **CATLG-VARS** **F3** **F1** **ENTER** **1** **)** to get the screen show on the top right.
6. Press **ENTER**. You should see the second screen on the right.

```
LinR (xStat,yStat y1)
█
```

```
LinReg
y=a+bx
a=-.33333333
b=1.5
↓corr=.981980506
█
CALC EDIT PLOT DRAW VARS
OneVd TwoVd LinR LnR Exe B
```

SUMMARY: FINDING THE LINE OF LEAST SQUARES FIT

1. Enter the data in xStat and yStat.
2. Press **2ND** **QUIT** to leave the lists.
3. Press **2ND** **STAT** **F1** **F3** to access the LinR.
4. Use the following format for LinR (xStat, yStat, y1). The keystrokes are outlines in step #4 above.
5. Press **ENTER** ..

FINDING EXTREMA (MAXIMA AND MINIMA)

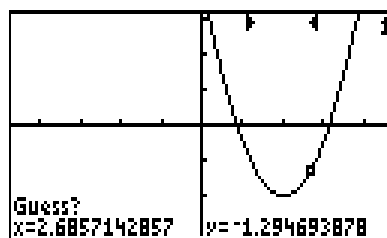
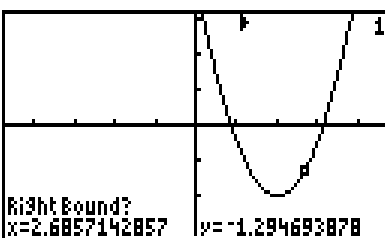
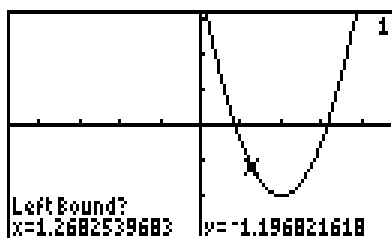
In Example 5, Section 3.1, we are asked to find the minimum point for the graph $f(x) = 1.5x^2 - 6x + 4$.

To find a minimum (or maximum) value:

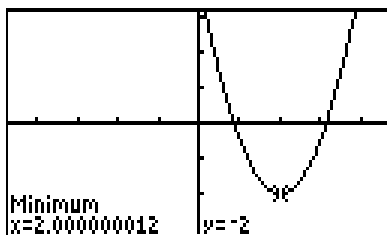
1. Enter and graph the function $f(x)$ using a viewing window of $[-4.7,4.7,1]$ by $[-3.1,3.1,1]$.
2. The last choice on the bottom row is **GRAPH** **▶**. Press **MORE**.
3. Press **F1** to access the **MATH** menu.
4. Press **F4** to select FMIN.
5. A graph is displayed with a blinking cursor and “Left Bound?” at the bottom of the screen. This is seen in the sequence of graphs below.
6. Position your cursor to the left of the vertex of the graph. Press **ENTER**.

7. In the “Right Bound?” screen position the cursor to the right of the vertex and press **ENTER**.

8. You will now see a screen with “Guess ?” . Press **ENTER**



9. The minimum point for this graph is (2.000000012, -2) as seen in the graph below.



Similar steps are used to find the maximum value of a function. The difference would be in the choice of **F4** in step #4 above.

To find the maximum value of a function press **F5** to select FMAX and follow the process as outlined above.

SUMMARY: FINDING EXTREMA (MAXIMA AND MINUMA)

1. Enter and graph the function $f(x)$ using an appropriate viewing window.
2. Press **MORE**.
3. Press **F1** to access the **MATH** menu.
4. Press **F4** to select FMIN. (Press **F5** to select FMAX).
5. When asked for a “Left Bound?” position your cursor to the left of the vertex of the graph and press **ENTER**.
6. In the “Right Bound?” screen position the cursor to the right of the vertex and press **ENTER**.
7. In the “Guess ?” screen press **ENTER**.
8. The calculator will display the coordinated for the minimum (or maximum) value.

FINDING A NONLINEAR FUNCTION OF LEAST-SQUARES FIT

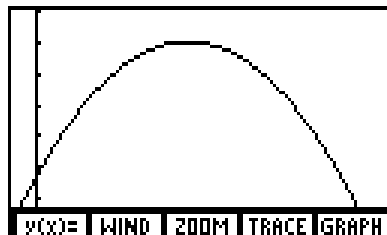
In Example 10, Section 3.1, a quadratic function of least-squares fit is found using steps similar to those used to find a line of least-squares fit.

To find a nonlinear function of least-squares fit:

1. Enter the data points found in Table 3.4 in xStat and yStat.
2. Press 2^{ND} **QUIT** to leave the lists.
3. Press 2^{ND} **STAT** followed by **F1**.
4. Press **MORE** to access additional functions.
5. Press **F4** to access P2Reg (quadratic regression function) This function fits the equation $y = ax^2 + bx + c$ to the data. P2Reg requires at least 3 data points. The format required by this function is P2Reg(xstat, ystat, y1).
6. Use the following keystrokes **(** 2^{ND} **LIST NAMES** **F2** , **F3** , 2^{ND} **CATLG-VARS** **F3** **F1** **ENTER** **1** **)** to get the screen show on the top right.
7. Press **ENTER**. You should see the screen on the right.
8. To see a graph of this function press the **GRAPH** key followed by the **F5** key. You may need to adjust your viewing window to fit the values in the table. To view the function press the **F1** key and use the right arrow cursor key to see the entire equation.

```
P2Reg (xStat,yStat,y1
)■
```

```
QuadraticReg
y=ax2+bx+c
n=14
PRegC=
(-.260756352252 6.69...
```



SUMMARY: FINDING A NONLINEAR FUNCTION OF LEAST SQUARES FIT

1. Enter the data points in xStat and yStat.
2. Press 2^{ND} **QUIT** to leave the lists.
3. Press 2^{ND} **STAT** **F1** **MORE** and **F4** to access P2Reg (quadratic regression function).
4. The format required is P2Reg(xstat, ystat, y1). The keystrokes are outlined in step #6 above.
5. Press **ENTER**.
6. Press **GRAPH** **F5** to view a graph of this function. Adjust the window as needed.
7. Press **F1** to view the equation.

SHADING BETWEEN TWO GRAPHS

In Example 4, Section 3.4, the region below the graph of $f(x) = -0.4x^2 + 4$ is shaded to make it appear like a mountain as illustrated in Figure 3.104.

To shade an area between two graphs:

1. Enter and graph the function. In this example we will use the standard viewing window.
2. Press **2ND** **QUIT** to return to the home screen.
3. Press **GRAPH** **MORE** and then **F2** to access the **DRAW** menu.
4. Press **F1** to select *Shade*. This command is also used to shade the area between two graphs. The format required by this command is `Shade(lower function , upper function , x left, x right)`. In this problem we do not have a lower function. Since the command will not shade in the region without a lower function select an arbitrary lower function. We will use -11 as our lower function since this value lies below the graph of $f(x)$ and does not appear in our viewing window.
5. Type `-11, -.4 x^2+4, -10, 10` where the last two values represent the `xMin` and `xMax` of the graph viewing window. Press **ENTER**.
6. The region under the curve should be shaded.

```
Shade(
```

```
Shade(-11, -.4 x^2+4, -10, 10
```

SUMMARY: SHADING A GRAPH

1. Enter and graph the function using an appropriate viewing window.
2. Press **2ND** **QUIT** to return to the home screen.
3. Press **GRAPH** **MORE** **F2** to access the **DRAW** menu.
4. Press **F1** to select *Shade*.
5. Enter a lower function , upper function , x left and x right value.
6. Press **ENTER** .

SETTING A DECIMAL WINDOW

In Example 3, Section 4.1, a decimal (or friendly) window is used to trace the graph of f . When we use the **ZDECM** setting the cursor stops on x values that are multiples of 0.1 .

To set a decimal window:

1. Press the **GRAPH** key followed by **F3** for the **ZOOM** menu.
2. Press the **MORE** key.
3. Press **F4** to select **ZDECM**.

COPYING A REGRESSION EQUATION INTO Y1

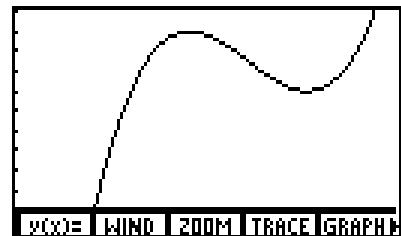
In Example 3, Section 4.2, a cubic regression was used to model real data.

To graph a regression equation:

1. Enter the data points in xStat and yStat.
2. Press 2^{ND} **QUIT** to leave the lists.
3. Press 2^{ND} **STAT** followed by **F1**.
4. Press **MORE** to access additional functions.
5. Press **F5** to access P3Reg (cubic regression function). The format required by this function is P3Reg(xstat, ystat, y1).
6. Use the following keystrokes $($ 2^{ND} **LIST** **NAMES** **F2** , **F3** , 2^{ND} **CATLG-VARS** **F3** **F1** **ENTER** **1** $)$ to get the screen show on the top right. This sequence of steps is identical to those used earlier to “find a nonlinear function of least squares fit”.
7. Press **ENTER**.
8. To graph this function press the **GRAPH** key followed by the **F5** key. You may need to adjust your viewing window to fit the values in the table.
9. To view the function press the **F1** key and use the right arrow cursor key to see the entire equation.

```
P3Reg (xStat,yStat,y1
)
```

```
CubicReg
y=ax3+bx2+cx+d
n=5
PRegC=
(.001584583431 -9.41...
```



SUMMARY: COPYING A REGRESSION EQUATION INTO Y1

1. Enter the data points in xStat and yStat.
2. Press 2^{ND} **QUIT** to leave the lists.
3. Press 2^{ND} **STAT** **F1** **MORE** to access the appropriate regression function.
4. The format required for a cubic regression formula is P3Reg(xstat, ystat, y1). A similar format is used for all regression formulas.
5. Press **ENTER**.
6. Press **GRAPH** **F5** to view a graph of this function. Adjust the window as needed.
7. Press **F1** to view the equation.

EVALUATING COMPLEX ARITHMETIC

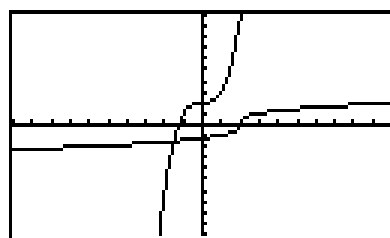
Complex numbers of the form $a + bi$ are entered into the graphing calculator as (a,b) . To add the complex numbers $(-2 + 3i) + (7 - 5i)$ you would enter $(-2,3) + (7,-5)$. Then press ENTER. The calculator returns the result $(5, -2)$ which would be then be written as $5 - 2i$. Other arithmetic operations are performed in a similar fashion.

GRAPHING AN INVERSE OPERATION

In Example 7, Section 5.2, the inverse function of $f(x) = x^3 + 2$ is graphed. You can use your graphing calculator to graph the inverse of a function without knowing the formula for $f^{-1}(x)$.

To graph the inverse of a function:

1. Enter $f(x)$ into the $y(x)=$ screen.
2. Press 2^{ND} **QUIT** to return to the home screen.
3. Press **GRAPH** **MORE** then **F2** to access the GRAPH DRAW menu.
4. Press the **MORE** key 3 times until you see DrInv in the bottom row.
5. Press **F3** to select the Drinv function. Enter the function.
6. Press **ENTER** to see a graph of both $f(x)$ and $f^{-1}(x)$



SUMMARY: GRAPHING AN INVERSE FUNCTION

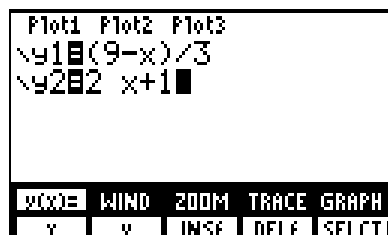
1. Enter $f(x)$ into the $y(x)=$ screen.
2. Press 2^{ND} **QUIT** to return to the home screen.
3. Press **GRAPH** **MORE** **F2** to access the DRAW menu.
4. Press the **MORE** key 3 times then **F3** to select the Drinv function.
5. Enter the function.
6. Press **ENTER** to see a graph of both $f(x)$ and $f^{-1}(x)$.

SHADING A SYSTEM OF INEQUALITIES

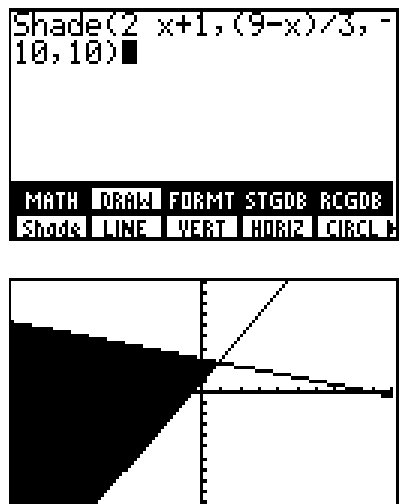
In Example 5(b), Section 6.2, we are asked to shade the solution set for a pair of inequalities $x + 3y \leq 9$ and $2x - y \leq -1$. In order to use these functions in our calculator we must first rewrite each inequality, expressing y in terms of x . These inequalities are rewritten as $y \leq (9-x)/3$ and $y \geq 2x + 1$.

To shade a system of inequalities:

1. Enter each function in the $y(x) =$ screen.
2. Press 2^{ND} **QUIT** to return to the home screen.
3. Press **GRAPH** **MORE** **F2** to access the **DRAW** menu.



- Press **F1** to select *Shade*. The format required by this command is $\text{Shade}(\text{lower function}, \text{upper function}, x \text{ left}, x \text{ right})$. In this problem the lower function is $y \geq 2x + 1$ since we are interested in the area above this line. The upper function is $y \leq (9-x)/3$ since we are interested in the area below this line.
- Type $2x + 1, (9 - x)/3, -10, 10$ where the last two values represent the xMin and xMax of the graph viewing window. Press **ENTER**.
- The region between the two lines should be shaded.



SUMMARY:SHADING A SYSTEM OF INEQUALITIES

- Enter each function in the $y(x) =$ screen.
- Press **2ND** **QUIT** to return to the home screen.
- Press **GRAPH** **MORE** **F2** to access the **DRAW** menu.
- Press **F1** to select *Shade*.
- Use the format $\text{Shade}(\text{lower function}, \text{upper function}, x \text{ left}, x \text{ right})$.to enter the required information.
- Press **ENTER** to see the region between the two inequalities shaded.

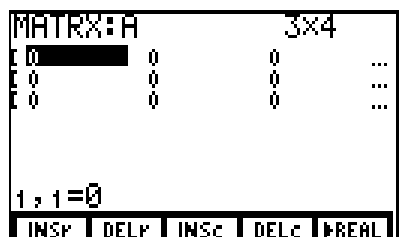
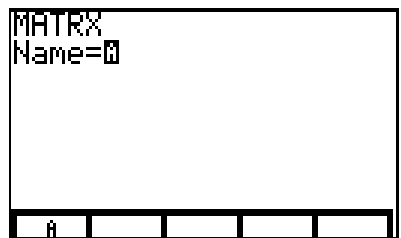
ENTERING THE ELEMENTS OF A MATRIX

In Example 8, Section 6.3, the elements of a matrix are entered into the graphing calculator. The augmented

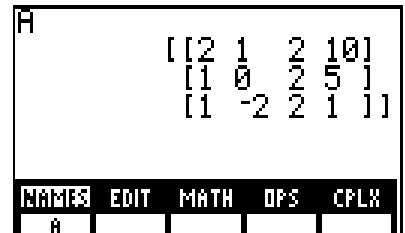
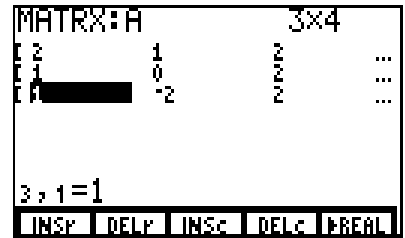
matrix A is given by $A = \left[\begin{array}{ccc|c} 2 & 1 & 2 & 10 \\ 1 & 0 & 2 & 5 \\ 1 & -2 & 2 & 1 \end{array} \right]$.

To create a matrix:

- Locate the word **MATRIX** over the number 7 on the calculator keypad. Press **2ND** **MATRIX** to access the **MATRIX** menu.
- Press **F2** to **EDIT**.
- To name the matrix select a letter of the alphabet (in this case A) and press **ENTER**.
- Enter the dimensions (*row X column*) of the matrix. Press **ENTER**.



- Begin entering the elements of the matrix. Press the **ENTER** key after each entry. The cursor moves to the next element.
- Press **2ND** **QUIT** to return to the home screen.
- To display the matrix press **2ND** **MATRIX** **F1** **F1** **ENTER**



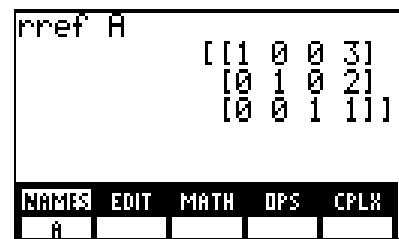
SUMMARY: CREATING A MATRIX

- Press **2ND** **MATRIX** to access the **MATRIX** menu.
- Press **F2** to create the matrix.
- Name the matrix. Press **ENTER**.
- Enter the dimensions (*row X column*) of the matrix. Press **ENTER**.
- Enter the elements of the matrix. Press **ENTER** after each entry.
- Press **2ND** **QUIT** to return to the home screen.
- To display the matrix press **2ND** **MATRIX** **F1** **F1** **ENTER**

REDUCED ROW ECHELON FORM

To transform a matrix into row reduced form:

- Press **2ND** **MATRIX** then **F4** to access the **OPS** (operations) menu.
- Press **F5** to select *rref*.
- Press **2ND** **M1** **F1** to select matrix **A**.
- Press **ENTER**.



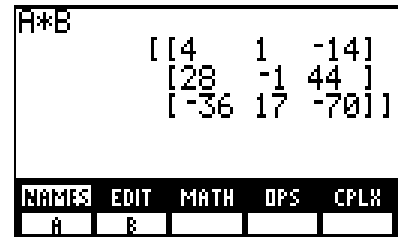
PERFORMING ARITHMETIC OPERATIONS ON MATIRCES

In Example 8, Section 6.4 the matrices **A** and **B** are multiplied. Begin by entering $A = \begin{bmatrix} 1 & 0 & 7 \\ 3 & 2 & -1 \\ -5 & -2 & 5 \end{bmatrix}$ and

$B = \begin{bmatrix} 4 & -6 & 7 \\ 8 & 9 & 10 \\ 0 & 1 & -3 \end{bmatrix}$ matrix **B** in your calculator using the instructions for creating a matrix.

To multiply two matrices:

1. Enter the matrices into the calculator.
2. Press **2ND** **QUIT** to return to the home screen.
3. Press **2ND** **MATRIX** **F1** **F1** then the multiplication sign then **F2**.
4. Press **ENTER**.



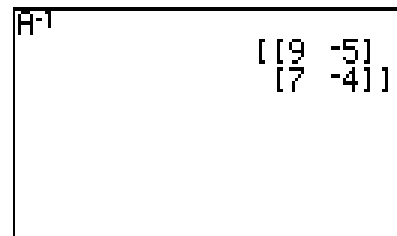
Other arithmetic operations are performed in a similar way.

FINDING THE INVERSE OF A MATRIX

In Example 4, Section 6.5 the inverse of $A = \begin{bmatrix} 4 & -5 \\ 7 & -9 \end{bmatrix}$ is found.

To find the inverse of a matrix

1. Enter the matrix into the calculator.
2. Press **2nd** **QUIT** to return to the home screen.
3. Press **2nd** **MATRIX** **F1** then select the matrix whose inverse you wish to find.
4. Press **2nd** **x⁻¹** (located above the **EE** key) followed by **ENTER**.

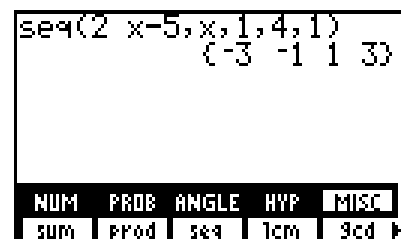
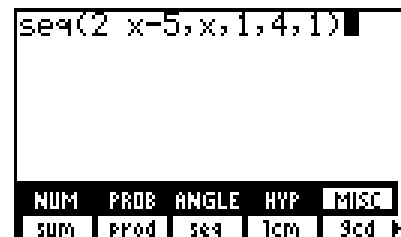


CREATING A SEQUENCE

A graphing calculator can be used to create a finite sequence of terms given a formula for the n^{th} term. We will generate the terms of the sequence $f(n) = 2n - 5$ for $n = 1, 2, 3, 4$.

To generate a finite sequence of terms:

1. Use the keystrokes **2ND** **MATH** to access the MATH menu .
2. Press **F5** to access the MATH MISC menu.
3. Press **F3** to select *seq*. The *seq* function returns a list in which each number in the list is the value of the formula evaluated for a given variable from beginning to end by step.
4. Enter the information as seen in the first screen on the right. The format used for the *seq* command is *seq(formula, variable, begin, end, step)*.
5. Press **ENTER**. The second screen shows the sequence of terms.



SUMMARY: CREATING A SEQUENCE

1. Use the keystrokes **2ND** **MATH** to access the MATH menu .
2. Press **F5** to access the MATH MISC menu.
3. Press **F3** to select *seq*.
4. Enter the information using the format $\text{seq}(\text{formula}, \text{variable}, \text{begin}, \text{end}, \text{step})$.
5. Press **ENTER** .

FIND THE SUM OF THE TERMS OF A SERIES

In Example 3, Section 8.2 the sum of the series $\sum_{n=1}^{50} \frac{1}{n^4}$ is found using the graphing calculator.

To find the sum of the terms of a series:

1. Use the keystrokes **2ND** **MATH** to access the MATH menu .
2. Press **F5** to access the MATH MISC menu.
3. Press **F1** to select *sum*. The sum function returns the sum of the elements of a list. Since the seq function will return a list of values for the summation given above we will take the sum of a sequence.
4. Press **F3** to select *seq* and enter the information using the format described in the section on creating a sequence.
5. Enter the information as seen in the first screen on the right.
6. Press **ENTER** . The second screen shows the sequence of terms.

```
SUM seq(1/x^4, x, 1, 50,
1)
NUM  PROB  ANGLE  HYP  MISC
SUM  PROD  SEQ  TCM  3rd
```

```
SUM seq(1/x^4, x, 1, 50,
1)
1.08232064598
NUM  PROB  ANGLE  HYP  MISC
SUM  PROD  SEQ  TCM  3rd
```

SUMMARY: FINDING THE SUM OF THE TERMS OF A SERIES

1. Use the keystrokes **2ND** **MATH** to access the MATH menu .
2. Press **F5** to access the MATH MISC menu.
3. Press **F1** to select *sum*.
4. Press **F3** to select *seq*.
5. Enter the information using the format $\text{seq}(\text{formula}, \text{variable}, \text{begin}, \text{end}, \text{step})$.
6. Press **ENTER** .

CALCULATING FACTORIAL NOTATION

In Example 5, Section 8.3, factorial notation is evaluated using the graphing calculator. Suppose we wish to find the numerical value of $8!$.

To calculate a factorial:

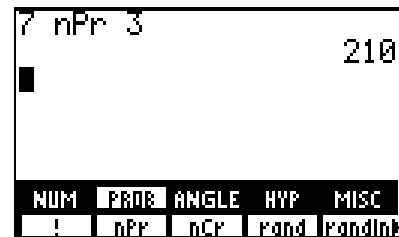
1. In the home screen type 8.
2. Use the keystrokes $\boxed{2ND}$ \boxed{MATH} to access the MATH menu .
3. Press $\boxed{F2}$ to access the MATH PROB menu.
4. Press $\boxed{F1}$ to select !.
5. Press \boxed{ENTER} .

CALCULATING PERMUTATIONS AND COMBINATIONS

In Example 6(a), Section 8.3, the permutation $P(7, 3)$ is evaluated. Suppose we wish to evaluate this permutation using the graphing calculator.

To calculate a permutation:

1. In the home screen type 7.
2. Access the \boxed{MATH} menu.
3. Press $\boxed{F2}$ to access the MATH PROB menu.
4. Press $\boxed{F2}$ again to select nPr.
5. Type 3.
6. Press \boxed{ENTER} .



In example 9(a), Section 8.3, the combination $C(7, 3)$ can be determined using the graphing calculator.

To calculate a combination:

1. In the home screen type 7.
2. Access the \boxed{MATH} menu.
3. Press $\boxed{F2}$ to access the MATH PROB menu.
4. Press $\boxed{F3}$ to select nCr.
5. Type 3.
6. Press \boxed{ENTER} .



GRAPHING PARAMETRIC EQUATIONS

To graph the parametric equations $x = t + 3$ and $y = t^2$ for $-3 \leq t \leq 3$.

To graph parametric equations:

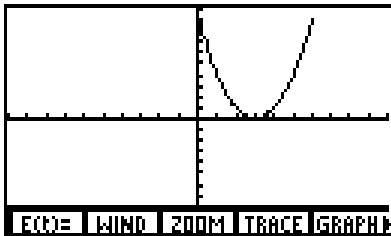
1. Press **2ND** **MODE**. Highlight Param and press **ENTER**. Check other settings to match those seen on the right.
2. Press **GRAPH** then **F1** to display the parametric equation options.
3. Enter the equations for x and y as seen on the right. Press **F1** to select the t variable.
4. Press **2ND** **M2** to set the window for your graph. Notice that you will need to set a tMin, tMax and tStep in addition to set values for x and y . tStep represents the increments between consecutive points plotted on the graph. A reasonable value for tStep = 0.1
5. Set an appropriate viewing window. In this problem use the default settings for x and y and $-3 \leq t \leq 3$ for the values for t .
6. Press **F5** to create the graph seen below.

```
Normal Sci Eng
Float 012345678901
Radian Degree
RectC PolarC
Func Pol Param DifEq
Dec Bin Oct Hex
RectC CylV SphereV
dxDer1 dxnDer
```

```
Plot1 Plot2 Plot3
\xt1t+3
yt1t^2

MODE WIND ZOOM TRACE GRAPH
t xt yt DELF SELCT
```

```
WINDOW
tMin=-3
tMax=3
tStep=.1
xMin=-10
xMax=10
↓xScl=1
MODE WIND ZOOM TRACE GRAPH
```



SUMMARY: GRAPHING PARAMETRIC EQUATIONS

1. Change your calculator to Parametric mode
2. Press **GRAPH** then **F1** to display the parametric equation options.
3. Enter the parametric equations for x and y . Use **F1** to select the t variable.
4. Set an appropriate viewing window for your graph. A reasonable value for tStep = 0.1
5. Press **F5** to view the graph.

GRAPHING IN POLAR COORDINATES

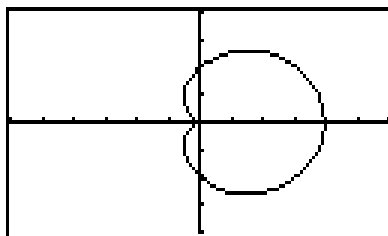
In Figure 8.92, Section 8.5 the polar equation $r = 2 + 2\cos \theta$ for $0^\circ \leq \theta \leq 360^\circ$ is graphed.

To graph polar equations:

1. Press **2ND** **MODE**. Highlight Pol and press **ENTER**. Set the calculator to Degree mode. Press **ENTER**.
2. Press **GRAPH** then **F1** to display polar equation options.
3. Enter the equation for r using **F1** to select θ .
4. Press **2ND** **M2** to set the window for your graph. Notice that you will need to set a θ Min, θ Max and θ Step in addition to values for x and y . θ Step represents the increments between consecutive points plotted on the graph. In degree mode a reasonable value for θ Step = 7.5.
5. Set an appropriate viewing window. In this problem use $-6 \leq x \leq 6$, $-4 \leq y \leq 4$ and $0^\circ \leq \theta \leq 360^\circ$ with θ Step = 7.5.
6. Press **F5** to view the graph.

```
Normal Sci Eng
Float 012345678901
Radian Degree
Rect Pol Arc
Func POL Param DifEq
Dec Bin Oct Hex
Rect Cyl SphereV
dxDer1 dxNDer
```

```
WINDOW
θMin=0
θMax=360
θStep=7.5
xMin=-6
xMax=6
↓xScl=1
F1(0)= WIND ZOOM TRACE GRAPH
```



SUMMARY: GRAPHING IN POLAR COORDINATES

1. Change the calculator to polar mode and select degree mode.
2. Press **GRAPH** then **F1** to display polar equation options.
3. Enter the equation for r using **F1** to select θ .
4. Set an appropriate viewing window. In degree mode a reasonable value for θ Step = 7.5.
5. Press **F5** to view the graph.